Spin accumulation encoded in electronic noise for mesoscopic billiards with finite tunneling rates
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We study the effects of spin accumulation (inside reservoirs) on electronic transport with tunneling and reflections at the gates of a quantum dot. Within the stub model, the calculations focus on the current-current correlation function for the flux of electrons injected into the quantum dot. The linear response theory used allows us to obtain the noise power in the regime of thermal crossover as a function of parameters that reveal the spin polarization at the reservoirs. The calculation is performed employing diagrammatic integration within the universal groups (ensembles of Dyson) for a nonideal, nonequilibrium chaotic quantum dot. We show that changes in the spin distribution determine significant alterations in noise behavior at values of the tunneling rates close to zero, in the regime of strong reflection at the gates.

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I. INTRODUCTION

The experimental control of electron transport in nanostuctures may lay the foundation for the development of devices for processing quantum information.1–3 These devices may rely on spin degrees of freedom, and are thus called spintronics.4 The control of spin is a subtle process that requires the fabrication of special samples, manipulating them so as to detect low-intensity currents in semiconductors.5–7

The accumulation of spin, when detected, allows the extraction of information of great value to the phenomenon of electron transport.1,8

To induce a spin polarization in a material sample that can be a reservoir of electrons, one creates a population of nonequilibrium spins with a finite interval of relaxation time. This population can be achieved through optical or electronic mechanisms. Routinely, the optical techniques require the injection of circularly polarized photons in order to transfer their angular momenta to electrons through a complex sample.9 The electronic injection involves the presence of magnetic electrodes connected to a sample, creating spin polarization in a nonequilibrium regime.3,4

Fluctuation properties of a nonequilibrium current indicate that just the average electronic currents are not enough for a complete description of the full quantum transport.9 The accumulation of spin in electronic reservoirs modifies the fluctuation properties of the nonequilibrium electronic current. Such a modification follows a mechanism proposed in Ref. 10, which reveals that noise power presents an asymmetry under reversal of the current and/or voltage in the presence of spin accumulation inside at least one reservoir. On the other hand, performing direct measurements of the fluctuations in semiconductor quantum dots can be a very hard task, precisely because the typical currents are of the order of nA and temperatures of the order of mK; very small indeed.

An experimental procedure found in Ref. 11, and justified theoretically in Refs. 12 and 13, is to perform the full counting statistics (FCS), which consists of counting the numbers of electrons and their degrees of freedom within a certain window of time. Real-time measurements can also be applied to study the spin transport properties on generic interfaces of heterostructures, according to the results in Refs. 14 and 15. Tunneling rates allow us to find not only the conductance, but also the shot noise (width of the conductance distribution).11

In the limit of high temperatures, noise provides information on the thermal fluctuation characteristics of dissipative systems. On the other hand, experimental measurements of noise at low temperatures, also known as shot noise, use tunneling rate in nonideal quantum transport,11 yielding important information about the discrete process of charge transmission.10 In mesoscopic systems both noise sources are present. A relevant parameter to measure the noise in quantum dots is the asymmetry factor $\alpha \equiv \langle G_i - G_j \rangle / \langle G_i + G_j \rangle$, with $G_i \equiv N_i \Gamma_i$, and $N_i$ and $\Gamma_i$ denoting, respectively, the number of open channels and the tunneling rate in the lead $i$. Therefore, the tunneling rates play a crucial role in mesoscopic systems and in measurements of noise.

Motivated by these recent advances in the noise measurements11 and by the asymmetry in current and/or tension seen in Ref. 10, we propose and study a myriad of possibilities to measure the spin accumulation in reservoirs through solely nonequilibrium electronic transport. This study is an alternative to that of active spin polarization in transport, which usually requires the presence of ferromagnetic leads,17 and measurement of spin polarization through spin current is, in principle, much more difficult than measuring tunneling in charge transport. For this, we consider the role of tunneling rates in the electronic transport for quantum dots coupled to reservoirs through normal guides. Considering independent electron spin distributions of these reservoirs, we show that the average noise displays new and surprising effects due to the asymmetry parameter $\alpha$. There are many theories for the calculation of electron counting statistics, including nonlinear $\sigma$ models (replica, supersymmetric, and Keldysh), quantum circuit theory, the cascade approach, the stochastic path integral technique, semiclassical methods based on solving Boltzmann-Langevin equations, etc. In this paper, we use one more method, proven to be powerful, based on the random matrix theory (RMT). More specifically, using RMT we study the generalization of the interesting experimental setup recently proposed in Ref. 10.
start by considering the time-dependent current \( \dot{I}_y(t) \) at lead \( y \), for \( y = 1,2,\ldots,m \), with \( m \) being the number of leads connected to the chaotic quantum dots. Within the framework of the scattering theory for quantum transport, the current-current correlation function can be written in the form \(^{16}\)

\[
\langle \delta I_y(t) \delta I_y(0) \rangle = \int \frac{dw}{2\pi} e^{-iw1} S_{\alpha\beta}(w),
\]

where \( \delta I_y(t) \equiv I_y(t) + \langle I_y(t) \rangle \) is the current fluctuation around the mean value \( \langle I_y(t) \rangle \). The Fourier transform of the current-current correlation function, Eq. (1), namely \( S_{\alpha\beta}(w) \), is the noise, which, in the absence of interaction, can be written as \(^{10}\)

\[
S_{\alpha\beta}(w) = \sum_{\gamma\nu} \sum_{(c_1, p)\in\gamma} \sum_{(c_2, q)\in\nu} \frac{e^{i\delta(\gamma\nu)}}{h} \int d\varepsilon A_{\gamma\nu}^{c_1,c_2\gamma}(\varepsilon; \varepsilon', \varepsilon') \times A_{\gamma\nu}^{c_2,p\gamma}(\varepsilon'; \varepsilon, \varepsilon') \left[f^{\alpha\beta}(\varepsilon) \left[1 - f^{\gamma\nu}(\varepsilon') \right] + f^{\gamma\nu}(\varepsilon') \left[1 - f^{\alpha\beta}(\varepsilon') \right] \right] + f^{\gamma\nu}(\varepsilon) f^{\alpha\beta}(\varepsilon') \equiv \epsilon + hw.
\]

The matrix

\[
A_{\gamma\nu}^{c_1,c_2\gamma}(\varepsilon; \varepsilon', \varepsilon') \equiv \delta_{c_1,c_2} \delta_{pq} \delta_{\alpha\gamma} \delta_{\nu\beta} - [S_{\alpha\beta}(w) S_{\beta\alpha}(w)]_{c_1,c_2; q} \text{ is the current matrix, where } S(\epsilon) \text{ is the scattering matrix, which can depend on the energy } \epsilon \text{ and describes the charge transport through the circuit.}
\]

Also, \( f^{\alpha\beta}(\varepsilon) = (1 + \exp((\epsilon - \mu_{\gamma\nu})/k_BT))^{-1} \) represents the Fermi distribution function, related to the thermal reservoir connected to the lead \( \alpha \). The sum in Eq. (2) extends over spin indices \( p, q = \pm \) polarizable along \( \mathbf{m}_y \), open channel indices \( c_1, c_2 \in \gamma \), and over all leads, including \( \alpha \) and \( \beta \).

The scattering matrix \( S(\epsilon) \) used to describe the mesoscopic system is uniformly distributed over the orthogonal ensemble if the system has both time-reversal and spin rotation symmetry, over the unitary ensemble if only time-reversal symmetry is broken by a intense external magnetic field, or over the symplectic ensemble if the spin rotation symmetry is broken by a intense spin-orbit interaction. \(^{26}\)

A particularly interesting limit of the resulting linear response theory occurs at zero frequency, for which there is a successful model established to treat noise of a phase-coherent conductor. \(^{23}\) In this limit, we define \( S_{\alpha\beta}(0) = S_{\alpha\beta}(0) \), and the transport is described in terms of external fields contained in the symmetries of the scattering matrices, the energies present in the corresponding Fermi distributions in the reservoirs, and the open channels in the leads. In the limit of both low temperatures and voltages, the scattering matrix is uniform within an energy window in the vicinity of the Fermi level, in a form such that the scattering matrix is given by \( S(\epsilon) = S(E_F) \), \( \forall \epsilon \), with \( E_F \) denoting the Fermi energy. From Ref. 27, along with the limits discussed above, spectral noise of the current-current correlation function function can be written as \(^{10,28}\)

\[
S_{\alpha\beta} = 2k_BT \left[ \delta_{\alpha\beta} 2N_{\alpha} - \text{Tr}(1 \rho S^1 \alpha S^1 \beta S) \right] + \frac{1}{4} \sum_{\gamma, \rho=1}^m \sum_{p,q=\pm} f_{\gamma\rho p}^{\rho\gamma} \left[ T_{\gamma\rho p}^{\rho\gamma} + 2p \text{Re} T_{\gamma\rho p}^{\rho\gamma} + pq T_{\gamma\rho p}^{\rho\gamma} \right].
\]

The matrix \( S \) has dimensions \( 2M \times 2M \), with \( M = \sum_{\gamma} N_{\gamma} \) denoting the total number of open channels in the leads. The
matrix $I_{\alpha}$ projects states on the transport guide $\alpha$. We also define
\begin{equation}
T_{\gamma\rho\delta\beta}^{ab} \equiv \text{Tr}[(1_{\gamma} \otimes \sigma^a)S^\dagger I_{a}(1_{\rho} \otimes \sigma^b)S^\dagger I_{b}S^\dagger],
\end{equation}
where $a, b \in \{0, z\}$ and $\sigma^z = \sigma \cdot m_\rho$, with $\sigma$ being the Pauli vector or matrix and $\sigma^0$ a $2 \times 2$ identity matrix.

B. Nonideal mesoscopic billiards

Now we present our new results, extending Ref. 10 to include tunneling and reflections. The scattering matrix incorporates the nonideal coupling between the ideal-channels of the leads and the internal modes of the QD. This coupling describes the tunneling rate $\Gamma_\alpha \in [0, 1]$ of the entrance and exit of the electronic modes of lead $\alpha$ in the QD. In RMT, the tunnel rate is generically referred to as a tunneling barrier. The presence of barriers requires a distribution of the scattering matrices within the Poisson kernel\textsuperscript{9,26,29,30} of RMT and integration in the Haar measure corresponding to extracting nonanalytical results for the averages. Therefore we will use the diagrammatic method proposed in Ref. 29 to find the leading term in the semiclassical expansion of the average noise. Following Refs. 29 and 31, the matrix $S$ can be parameterized by the stub model, being composed of an average part $R$ and a fluctuating part $\delta S$:
\[ S = R + \delta S, \quad \delta S = T[1 - RU]^{-1}UT. \]

The matrix $U$ is random orthogonal, and unitary or symplectic depending on the Dyson ensemble, with dimensions $2M \times 2M$. The matrices $T$ and $R$ are diagonal $2M \times 2M$ matrices, given by $T = \text{diag}(i\sqrt{\Gamma_{m1}1_{2N_{1}}}, \ldots, i\sqrt{\Gamma_{m2N_{2}}1_{2N_{2}}})$ and $R = \text{diag}(i\sqrt{\Gamma_{g1}1_{2N_{1}}}, \ldots, i\sqrt{\Gamma_{g2}1_{2N_{2}}})$.

In the limit of many open channels $M \gg 1$, we can expand $S$ in powers of $U$ and perform a diagrammatic integration, obtaining average moments of the scattering matrix in the Poisson kernel. According to Eq. (3), the average noise requires the calculation of the semiclassical expansion of the trace of products of two and four scattering matrices. We performed the calculation and verified explicitly that only the ladder diagrams (difusons) contribute to the leading term of the average noise. The diagrams for the average over the trace of the product of two matrices $S$ can be found in Ref. 29, while the diagrams for obtaining the average of four matrices $S$ can be found in Ref. 31. We get, for a ballistic chaotic quantum dot connected to multiple terminals, the following known general result:
\[ \langle \text{Tr}(1_{\beta}S^\dagger I_{\alpha}S) \rangle = 2\delta_{\alpha\beta}[N_{\beta} - G_{\beta}] + 2G_{\beta}G_{\alpha}G_{T}^{-1}. \]

The average of Eq. (4) is calculated in a generic form for any ensemble, an arbitrary number of leads, and different tunneling rates in each lead. We obtain the following new result, valid for the universal ensembles:
\[ \langle T_{\gamma\rho\delta\beta}^{ab} \rangle = 2\delta_{ab} \left\{ \delta_{\gamma\rho\delta\beta}(N_{\gamma} - 2G_{\gamma} + G_{\gamma}T_{\gamma\rho\delta\beta}) + \delta_{\alpha0}G_{\gamma}G_{\alpha}G_{\beta}G_{T} + \frac{G_{\gamma}G_{\alpha}G_{\beta}}{G_{T}} \left[ 2 - \Gamma_{\gamma} - \Gamma_{\alpha} - \Gamma_{\rho} - \Gamma_{\beta} + \delta_{\rho0}G_{\gamma}G_{\alpha}G_{\beta} \right] \right\}, \]

where $G_m = N_m\Gamma_m$, $G_T = \sum_{m=1}^{N} G_m$, and $\gamma, \alpha, \rho, \beta = 1, \ldots, m$. In unitary or symplectic ensembles, we consider the noncolinear spin accumulation in the direction of the unit vectors $m_\gamma$, $m_\alpha$, $m_\rho$, $m_\beta$ such that we replace $m_\gamma \cdot m_\rho \to \delta_{\gamma\rho}$, where $a = z = b$. In the orthogonal case, we should take $\delta_{\alpha0} \to 1$ owing to both spin rotation and time-reversal symmetries. In the case of absence of spin accumulation, for which Eqs. (5) and (6) can be used with $a = 0 \neq b$, we recover the known results of the literature.\textsuperscript{32} We also recover the ideal contacts case, $\Gamma_\gamma = 1$, in the presence of spin accumulation obtained in Ref. 10 for the average noise. Our general result is the main (semiclassical) term of the average noise, and it is valid for three ensembles of Dyson. Without loss of generality, we focus on the unitary ensemble and study surprising asymmetries due to tunneling rates. Sample-to-sample measurements can lead to the corrections discussed in Ref. 10, which give rise to other noise asymmetries from the $T_{\gamma\rho\delta\beta}$ term in Eq. (3) (zero, on average).

III. ELECTRONIC NOISE POWER AND SPIN ACCUMULATION IN RESERVOIRS

The previous results are general and apply to the case of many terminals coupled to the QD. In this section, we analyze the more widely studied case of noise in the regime of spin accumulation in a ballistic QD coupled to two leads with nonideal contacts, as described in Fig. 1. We study in detail the two-terminal case, having in mind the curious and surprising fact that this configuration presents a clear instance of nonequilibrium spin accumulation phenomena, which is quite interesting for direct phenomenology and investigations of noise. Let us consider a number of open channels $N_1$ and $N_2$ in the leads connected to the reservoirs labeled 1 and 2, respectively. Without loss of generality, we assume that the accumulation of spin occurs only in reservoir 1 so that $\Delta \mu_1 = eV + p\delta \mu$ and $\Delta \mu_2 = 0$ in the Fermi distribution. Substituting the general Eqs. (5) and (6) in Eq. (3), we get
the expression for the two-terminal case:

\[
\frac{\langle S_{11} \rangle}{k_BT} = \frac{6G_1G_2}{G_T^2} + \frac{G_1G_2\Gamma_1(2G_2 + G_1)}{G_T^2} + \frac{4G_1^2\Gamma_1 + 3G_1^2\Gamma_2}{G_T^2} + |\Delta| \coth(|\Delta|) \left[ G_1^2 G_2^2 (2 - \Gamma_1) + \frac{2G_1G_2^2(1 - \Gamma_1)}{G_T^2} + \frac{G_1^2 \Gamma_2}{G_T^3} \right] + \left[ \Phi + \Delta \left( \frac{\Phi + \Delta}{2} \right) + \Phi - \Delta \left( \frac{\Phi - \Delta}{2} \right) \right] \left[ G_1G_2^2 + G_3^1(1 - \Gamma_2) + G_3^2(1 - \Gamma_1) \right].
\]

with \( \langle g \rangle = 2G_1G_2/G_T, \ \Phi = eV/k_BT, \) and \( \Delta = \delta\mu/k_BT. \)

We also show that this equation satisfies the conservation law

\( S_{1i} = -S_{2i}, \) with \( i = 1, 2, \) indicating that the behavior of any \( S_{ij} \) is identical.

Before we analyze Eq. (7), we should first verify several of its basic limits. We start by considering the limit \( k_BT \gg eV, \delta\mu \) and obtain the universal thermal noise

\( \langle S_{11} \rangle = \frac{4k_BT}{\langle g \rangle}. \) Another important case which leads to the shot-noise power is the limit \( eV \gg \delta\mu, k_BT, \) through which we find that

\[
F = \frac{\langle S_{11} \rangle}{2eI},
\]

where \( F \) is the Fano factor and \( 2eI \) is the Poisson noise:

\[
F = \frac{G_1G_2}{G_T^2} + \frac{G_1^2(1 - \Gamma_2) + G_2^2(1 - \Gamma_1)}{G_T^2}.
\]

From Eq. (8), we can see that in the case of symmetric contacts, \( G = G_1 = G_2 \) and \( \Gamma_1 = \Gamma_2 = \Gamma, \) the Fano factor simplifies to \( F = 1/4 \times (2 - \Gamma) \) under a typical ballistic QD, for which \( F = 1/4 \) in the case of ideal contacts. It is also possible to see in Eq. (7) that the noise is nonzero even when \( eV \to 0 \) for an arbitrary value of temperature crossover. The spin accumulation maintains the noise for arbitrary electrochemical potentials for both shot-noise power and thermal noise power. The general Eq. (7) in the case of symmetric contacts simplifies to the following expression:

\[
\frac{\langle S_{11} \rangle}{k_BT} = \frac{6 + 5\Gamma}{4} + \frac{2 - \Gamma}{4} \times \left[ |\Delta| \coth(|\Delta|) + |\Phi + \Delta| \coth \left( \frac{|\Phi + \Delta|}{2} \right) \right] + |\Phi - \Delta| \coth \left( \frac{|\Phi - \Delta|}{2} \right).
\]

The behavior of Eq. (9) is displayed in Fig. 2. In the left panel, we fix \( \Phi \) at a fixed generic value and also fix several values of the barriers. We observe in this figure that the barrier greatly amplifies the signal of \( \langle S_{11} \rangle/k_BT \langle g \rangle. \) We observe two

![FIG. 2. (Color online) We depict the behavior of the noise and its first derivative in the regime of spin accumulation as a function of tunneling rate \( \Gamma \) in a quantum dot with nonideal symmetrical contacts. For \( \Delta > \Phi, \) we observe that the noise suffers abrupt changes, enhanced by the finite tunneling rates.](115123-4)
anomalous characteristics of the first derivative: The first is centered at the inversion point of the spin polarization of the reservoir, and the second is in the region of saturation at which $\Phi = \Delta$. In these zones drastic changes of the rate of increase in the noise occur, encoded in the value of its first derivative, which stabilizes between two plateaus as the bias voltage decreases. In the right panel, we investigate the finite value of $\Gamma_1 \lesssim 0.5$ of the tunneling rate and the disappearance of one of the plateaus. The elimination of one of the plateaus of the first derivative indicates that the tunneling rate has an important role in the study of the saturation zone as the bias voltage is decreased. It is one of the important effects of the tunneling rate on the spin accumulation in the system. Taking the limit $\delta \mu \gg eV, k_B T$, we obtain

$$\frac{\langle S_{11} \rangle}{\langle g \rangle} = \frac{3}{4} (2 - \Gamma) |\delta \mu|,$$

which can be rewritten in terms of the Fano factor as $\langle S_{11} \rangle/\langle g \rangle = 3 \times F \times |\delta \mu|$.

### IV. OPAQUE LIMIT

A particularly interesting regime in experiments involving tunneling rates is called the “opaque limit.” The experimental data in real-time traces of Refs. 11, 14, and 15 are basically in this category. The opaque limit is well-defined in Ref. 33, where analytical calculations using a semiclassical method were performed, allowing the acquisition of time scales typical of transport phenomena in ballistic cavities. This regime is defined by taking limits of $N_\alpha \to \infty$ and $\Gamma_\alpha \to 0$ such that $G_\alpha$ be finite. Taking this limit, the general expression (7) simplifies to the equation

$$\frac{\langle S_{11} \rangle}{k_B T \langle g \rangle} = \frac{(1 - a^2)}{2} \left[ 3 + |\Delta| \coth(|\Delta|) \right]$$

$$+ \frac{(1 + a^2)}{2} \left[ |\Phi + \Delta| \coth \left( \frac{|\Phi + \Delta|}{2} \right) \right]$$

$$+ |\Phi - \Delta| \coth \left( \frac{|\Phi - \Delta|}{2} \right),$$

(11)

where we have defined $a \equiv (G_1 - G_2)/G_T$, thus totally encoding the open channels. The entrance and exit events of the QD are uncorrelated and the asymmetric parameter $a$ of the tunneling rate was used in Ref. 11 to designate the normalized moments of a single level in the QD.

In Fig. 3, we analyze how the tunneling rates affects the noise, Eq. (7), through the $a$ parameter. Note that for ideal contacts, $\Gamma_1 = \Gamma_2 = 1$, the noise is highly asymmetrical with respect to this parameter. This asymmetry is a result of the spin accumulation in QD, considering that the noise is always symmetrical with respect to $a$ in the absence of spin accumulation, regardless of the values of $\Gamma_1$ and $\Gamma_2$. A similar asymmetry effect owing to the topology of the QD was reported in Ref. 34. In the other curves shown in Fig. 3 we present the behavior of the noise when we vary the values of the parameters $\Gamma_1$ and $\Gamma_2$ till we reach the opaque limit, $\Gamma_{1,2} \to 0$. In the transition between the two regimes,

![Fig. 3. (Color online) We depict the behavior of the noise in the regime of spin accumulation as a function of the tunneling rate $\Gamma$ in a QD with nonideal contacts, through the parameter $a = (G_1 - G_2)/G_T$. Note that for ideal contacts, $\Gamma_1 = \Gamma_2 = 1$, the noise is highly asymmetrical with respect to this parameter. In the other curves we vary the values of $\Gamma_1$ and $\Gamma_2$ till we reach the opaque limit, $\Gamma_{1,2} \to 0$. In this case the noise becomes symmetrical with respect to $a$.](115123-5)
we found that decreasing the tunneling rates has the effect of symmetrizing the noise. Surprisingly, in the opaque limit the noise becomes symmetric with respect to $a$ even in the presence of spin accumulation at any value of $\Delta$. Namely, the opaque limit symmetrizes the noise with spin accumulation, and the control parameter responsible for this transition is the tunneling rate exemplified by $\Gamma_i$. In addition, once again we find that, for values such that $\Delta > \Phi$, the noise remained stationary in terms of $a$.

We note here that the ideal-opaque transition, determined by the finite value of the tunneling rate, also inverts the concavity of the noise signal. The second derivative of the noise as a function of the asymmetry parameter can be written as

$$\frac{\partial^2}{\partial a^2} \langle S_{11} \rangle_{a} = f(a, \Gamma_1, \Gamma_2) \times g(\Phi, \Delta),$$

where $f(a, \Gamma_1, \Gamma_2) \equiv 4 + 3\Gamma_1(a - 1) - 3\Gamma_2(a + 1)$ and $g(\Phi, \Delta)$ is a function of $\Phi$ and of $\Delta$. We observe that the sign of the second derivative is fixed by the sign of $f$. We separate the diagram generated by $\Gamma_1 \times \Gamma_2$ into three distinct regions according to the sign (+) and (−) as exhibited in Fig. 4. The (+) and (−) regions determine, respectively, upward or downward concavity, whereas (+/−) determines a change of concavity in the sign of the noise power in $a \in [-1, 1]$. Note that these regions are separated by the straight lines $\Gamma_1 = 2/3$ and $\Gamma_2 = 2/3$ in the diagram. The particular case of the ideal, maximum tunneling rate is a vertex of the diagram situated in the (−) region, whereas the opaque, zero tunneling limit is close to the vertex in the neighborhood of the (+) region in the diagram.

Finally, we consider the limit $eV, \delta\mu \gg k_B T$ in Eq. (11). This limit allows us to get the shot noise given by the expression

$$\frac{\langle S_{11} \rangle}{\langle g \rangle} = \frac{1}{2}(1 + a^2)\left|eV + \delta\mu\right| + |eV - \delta\mu| + \frac{1}{2}|\delta\mu|,$$

$$\frac{\langle S_{11} \rangle}{\langle g \rangle} = \frac{1}{2}(1 + a^2)\left|eV\right|, \quad eV \gg \delta\mu,$$

$$\frac{\langle S_{11} \rangle}{\langle g \rangle} = \frac{3}{4}|\delta\mu|, \quad \delta\mu \gg eV.$$
of the noise as a function of the asymmetry parameter, and have shown that only the opaque limit is totally symmetrical with well defined concavity. We have also exhibited results showing the effect of the tunneling rate on the saturation of the spin accumulation, which is potentially of experimental value as it shows the effects of the induced potentials due to the spin accumulation.

In Ref. 14 it was shown that fine adjustment of the voltage gates can alter the orbital configuration of the QD, restoring the tunneling between resonant levels of excited spin states in the presence of a magnetic field. An asymmetry parameter was used in Ref. 11 to obtain the noise in the presence of finite tunneling rates. Typical values used in that reference were in the range 1000–10000 Hz, generating a clear noise signal as a function of the asymmetry parameter. We performed an analysis of the correction to the shot-noise power and the Fano factor, resulting from the spin accumulation, in terms of reflections at the gates and the asymmetry parameter. Our findings may facilitate the experimental study of spin accumulation in reservoirs of mesoscopic systems in general. Other recent studies including electron-electron interaction or capacitance can be investigated considering barriers and spin accumulations.35

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